

A Geometrical 1% Distance to the Short-period Binary Cepheid V1334 Cygni

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Received 2018 August 8; revised 2018 September 16; accepted 2018 September 19; published 2018 November 6

Abstract

Cepheid stars play a considerable role as extragalactic distances indicators, thanks to the simple empirical relation between their pulsation period and their luminosity. They overlap with that of secondary distance indicators, such as Type Ia supernovae, whose distance scale is tied to Cepheid luminosities. However, the period-luminosity (P–L) relation still lacks a calibration to better than 5%. Using an original combination of interferometric astrometry with optical and ultraviolet spectroscopy, we measured the geometrical distance $d = 720.35 \pm 7.84$ pc of the 3.33 day period Cepheid V1334 Cyg with an unprecedented accuracy of $\pm 1\%$, providing the most accurate distance for a Cepheid. Placing this star in the P-L diagram provides an independent test of existing P-L relations. We show that the secondary star has a significant impact on the integrated magnitude, particularly at visible wavelengths. Binarity in future high-precision calibrations of the P–L relations is not negligible, at least in the short-period regime. Subtracting the companion flux leaves V1334 Cyg in marginal agreement with existing photometric-based P-L relations, indicating either an overall calibration bias or a significant intrinsic dispersion at a few percent level. Our work also enabled us to determine the dynamical masses of both components, $M_1 = 4.288 \pm 0.133 M_{\odot}$ (Cepheid) and $M_2 = 4.040 \pm 0.048 M_{\odot}$ (companion), providing the most accurate masses for a Galactic binary Cepheid system.

Key words: binaries: close - binaries: spectroscopic - stars: variables: Cepheids - techniques: high angular resolution techniques: interferometric - techniques: radial velocities

1. Introduction

Cepheids play a particularly important role as extragalactic distance indicators thanks to the empirical relation between their pulsation period and their luminosity: the periodluminosity (P-L) relation or Leavitt law (Leavitt & Pickering 1912). The ability to predict their intrinsic luminosity from their variation period makes them precious standard candles, as its combination with their measured apparent magnitude gives the distance modulus in a simple, empirical manner. Cepheids are radially pulsating, young and bright supergiant stars that are easily identified in distant galaxies (≤25 Mpc). Their distance scale overlaps with secondary distance indicators, such as supernovae Ia (SNIa), whose distance scale is securely tied to Cepheid luminosities. Therefore, an accurate and precise calibration of the Cepheid luminosities is necessary to ensure a reliable calibration for the secondary distance indicators. However, despite considerable efforts over more than one century, the calibration of the zero-point (ZP) of the P-L relation has not yet reached a 1% accuracy level. A better control of the systematic uncertainties is needed to establish the

P-L relation calibration at this level, and secondary effects on the photometric measurements such as a metallicity-dependence or interstellar reddening must be understood and taken into consideration.

It is now clear that the intrinsic scatter of the relation is smaller at longer wavelengths (see e.g., Freedman & Madore 2010; Madore & Freedman 2012) than it is for V-band $(\sim 0.5 \,\mu\text{m})$ measurements. In optical bands, the line-of-sight extinction is stronger than in the infrared (IR), and flux contamination from any main-sequence companion is likely to be larger-from an evolutionary timescale point of view, most of the companions should be stars close to the main-sequence (see e.g., Bohm-Vitense 1985; Evans 1992; Szabados & Klagyivik 2012). As they are relatively massive stars, the binary fraction of Cepheids is known to be at least 50% (Szabados 2003), and the presence of companions may bias the calibration of the P-L relation if their photometric contribution is not removed (Szabados & Klagyivik 2012; Gaia Collaboration et al. 2017). Furthermore, this bias is likely not constant as a function of the pulsation period as the bright long-period Cepheids (hence massive) have a higher contrast with their companions (reducing the potential photometric bias) compared to the shortest periods (less massive), but they are also more likely to be members of multiple stars systems with more massive companions than are short-period Cepheids (see e.g., Sana & Evans 2011, increasing the bias). In the near- and mid-IR, Cepheids usually strongly overshine their companions, and such effects are reduced. On the other hand, the presence of circumstellar envelopes increases the measured flux beyond that of the Cepheid itself (\lesssim 5% and 1%–30% of IR excess in the near- and mid-IR, respectively), and so systematically affects the distance estimates (Kervella et al. 2006; Mérand et al. 2006; Gallenne et al. 2013a, 2017). The optimal band seems to be the K band (~2.2 μ m) where the contributions of both the companions and the envelopes are mitigated, but the Cepheid distance scale must nevertheless be tested at the percent level. Such a test seems to be even more critical with the growing evidence of a $\sim 3.7\sigma$ discrepancy between the value of the Hubble constant H_0 predicted from cosmic microwave background anisotropies (Planck Collaboration et al. 2018) and the recent empirical calibration using Cepheids and SNIa (Riess et al. 2016). Before invoking new physics in the standard cosmological model, new high-accuracy data are necessary.

For now, the calibration of the P-L relation is partially anchored to 17 Galactic Cepheids having trigonometric parallax measurements, obtained from the Hubble Space Telescope (HST) Fine Guidance Sensor (Benedict et al. 2007, 2002; 10 Cepheids) and Wide Field Camera 3 spatial scanning (Riess et al. 2018; 7 Cepheids). Unfortunately, their average accuracy is limited to 8%, preventing a reliable 1% calibration of their luminosity. While the final Gaia data release expected in 2022 will provide hundreds of Cepheid parallaxes to 3% or less, our knowledge of the interstellar extinction will still be an important limitation to derive highly accurate Cepheid luminosities. In addition, close orbiting companions could bias the Gaia astrometric measurements and therefore, the resulting parallaxes, if they are assumed to be single stars (see e.g., Anderson et al. 2016b). Here we report the determination of the geometrical distance of the Galactic binary Cepheid V1334 Cyg with a very high accuracy of 1%, providing the most accurate anchor point of the P-L relation for short-period Cepheids. Our observations also enable us to confirm and measure the bias due to the companion on P-L calibrations.

Binary Cepheids offer the opportunity to measure accurate distances and masses through the combination of astrometric (visual orbit) and spectroscopic (radial velocities (RVs)) measurements. But this is a challenging task because of (1) the small angular size of the orbits, which hampers astrometric measurements using single-dish telescopes, and (2) the high contrast between the Cepheid and its companion, which complicates the detection of the companion's spectral lines and the measurement of its RV. Despite these difficulties, we report in the present work the detection of both the Cepheid and secondary component of V1334 Cyg using interferometric as well as visible and ultraviolet (UV) spectroscopic observations. This system was the first target chosen for our interferometric observing campaign, first because the expected H-band contrast between the components is reachable by the current interferometric combiners, and also because the spectroscopic orbit is particularly well known (Evans 1992, 2000). We present in Section 2 all of the data we collected for the V1334 Cyg system. In Section 3 we introduce the models we

 Table 1

 H-band Uniform Disk Sizes of Calibrators

as) (mag)	(mag)
± 0.032 5.87	4.87
± 0.043 6.65	4.46
± 0.049 4.22	3.86
± 0.031 5.59	4.86
± 0.040 5.52	4.44
£ 0.031 6.18	4.97
± 0.050 6.11	4.16
± 0.034 6.68	4.67
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used to fit our observations and derive our orbital solutions. We then discuss and conclude our results in Section 4.

2. Observations and Data Reduction

2.1. Interferometry

The relative astrometric positions of the companion of V1334 Cyg were measured repeatedly using interferometric observations performed with the Michigan Infrared Combiner (MIRC; Monnier et al. 2004), installed at the Center for High Angular Resolution Astronomy array (ten Brummelaar et al. 2005) located on Mount Wilson, California. The array consists of six 1 m aperture telescopes with an Y-shaped configuration (two telescopes on each branch), oriented to the east, west, and south, and so offering a good coverage of the (u, v) plane. The baselines range from 34 to 331 m, providing an angular resolution down to 0.5 mas in H. The MIRC instrument combines the light coming from all six telescopes in the H band, with three spectral resolutions (R = 42, 150, and 400). The recombination of six telescopes gives simultaneously 15 fringe visibilities and 20 closure phase measurements, which are our primary observables. Our observations were carried out from 2012 July to 2016 October using either four, five, or six telescopes. We used the low spectral resolution mode, where a prism splits the light on the detector into eight narrow spectral channels. We followed a standard observing procedure, i.e., we monitored the interferometric transfer function by observing a calibrator before and after our Cepheids. The calibrators were selected using the SearchCal software¹⁷ (Bonneau et al. 2006) provided by the Jean-Marie Mariotti Center. They are listed in Table 1.

The data were reduced with the standard MIRC pipeline (Monnier et al. 2007). The main procedure is to compute squared visibilities and triple products for each baseline and spectral channel, and to correct for photon and readout noises.

For each epoch, astrometric position were determined by fitting squared visibilities (V^2) and closure phases (CP) with our dedicated tool CANDID (Gallenne et al. 2015), with errors estimated using the bootstrapping technique (with replacement and the 1000 bootstrap sample). At each epoch, the fitted parameters are the relative astrometric position ($\Delta \alpha$, $\Delta \delta$), the uniform disk (UD) angular diameter of the primary θ_{UD} , and the flux ratio between the components *f*. The equation for the complex visibility for a binary system with an unresolved

¹⁷ Available at http://www.jmmc.fr/searchcal.



Figure 1. χ_r^2 map of the local minima (left) and detection level map (right) of V1334 Cyg for the 2012 July observations. The yellow lines represent the convergence from the starting points to the final fitted position, as explained in Gallenne et al. (2015). The maps were re-interpolated in a regular grid for clarity. The axis limits were chosen according to the location of the companion.

companion is

$$V(u, v) = \frac{V_{\star}(u, v) + fV_{c}(u, v)}{1 + f}$$
$$V_{\star}(u, v) = \frac{2J_{1}(\pi\theta_{\text{UD}}B/\lambda)}{\pi\theta_{\text{UD}}B/\lambda}$$
$$V_{c}(u, v) = \exp[-\frac{2i\pi}{\lambda}(u\Delta\alpha + v\Delta\delta)]$$
$$\phi_{iik} = \arg[V(u_{i}, v_{i})V(u_{j}, v_{j})V^{*}(u_{k}, v_{k})]$$

where $V_{\star}(u, v)$ and $V_{c}(u, v)$ are the complex visibilities of the Cepheid and companion, respectively, J_1 the first-order Bessel function, (u, v) the spatial frequencies, B the baseline between two telescopes (i, j), λ the observing wavelength, and ϕ_{iik} the closure phase for each closed baseline triangle (i, j, k). More details about the companion search formalism with CANDID are available in Gallenne et al. (2015, 2013b). Briefly, the tool provides a 2D-grid of fit using a least-squares algorithm. For each starting point in the grid, a multiparameter fit is performed, i.e., adjusting $\Delta \alpha$, $\Delta \delta$, $\theta_{\rm UD}$, and f. Each position of the grid leads to a local minimum. If the starting grid is fine enough (estimated a posteriori), multiple starting points lead to the same local minima, guaranteeing that all the local minima are explored. The deepest location identifies the best local minimum. Figure 1 shows the map of the local minima of the reduced χ^2 for our first observing epoch, in which the companion is detected at more than 50σ . The measured astrometric positions are listed in Table 2.

These observations also provide us with the diameter of the Cepheid at various epochs of its pulsation phase. However, the angular diameter variation is at most 0.02 mas for such a shortperiod Cepheid. Visibility measurements with an accuracy better than 2% would be required to detect such a variation, and this is well below the average MIRC accuracy for a 4.7 mag star. We therefore determined the average UD diameter simply by calculating the mean and standard deviation of our measurements. The conversion from UD to limb-darkened (LD) angular diameter is done using a linear-law parameterization with the LD

 Table 2

 Measured Astrometric Positions and Flux Ratio (H band) of the Companion of V1334 Cyg

MJD	$\Delta \alpha$ (mas)	$\Delta\delta$ (mas)	f (%)
56135.461	-1.140 ± 0.142	-8.832 ± 0.043	3.39 ± 0.60
56201.211	-0.099 ± 0.029	-8.365 ± 0.023	3.32 ± 0.37
56505.474	4.450 ± 0.116	-3.695 ± 0.050	2.99 ± 0.52
56560.226	4.935 ± 0.008	-2.615 ± 0.010	3.19 ± 0.16
56855.307	5.818 ± 0.023	3.786 ± 0.024	2.89 ± 0.26
56860.413	5.815 ± 0.033	3.844 ± 0.028	3.31 ± 0.46
56862.406	5.744 ± 0.028	3.937 ± 0.025	3.31 ± 0.15
56931.307	5.094 ± 0.027	5.062 ± 0.018	3.45 ± 0.35
57228.411	-1.280 ± 0.064	4.306 ± 0.037	3.08 ± 0.25
57235.412	-1.398 ± 0.022	4.130 ± 0.014	3.12 ± 0.15
57587.410	-6.008 ± 0.035	-4.987 ± 0.042	4.26 ± 0.58

coefficient $u_{\lambda} = 0.2423$, as explained in Gallenne et al. (2013b). We measured $\theta_{\text{LD}} = 0.524 \pm 0.039$ mas. Combined with our measured distance, we estimate the linear radius of the Cepheid to be $R_1 = 40.6 \pm 3.0 R_{\odot}$.

2.2. Visible Spectroscopy

High quality optical spectra were collected using the fiberfed high-resolution SOPHIE and HERMES spectrographs (Bouchy et al. 2009; Raskin et al. 2011). A total of 14 measurements have been obtained from 2013 to 2016 with SOPHIE, mounted on the 1.93 m telescope of the Observatoire de Haute Provence (France). The instrument covers visible wavelengths with a spectral resolution of $R \sim 75,000$ (highresolution mode). We also collected 56 spectra from 2010 to 2017 with HERMES ($R \sim 85,000$), mounted on the Flemish 1.2 m telescope of the Roque de los Muchachos Observatory (La Palma, Canary Islands). Exposure times of a few minutes allowed a signal-to-noise ratio per pixel at 550 nm > 50. Data were reduced using the dedicated HERMES and SOPHIE pipelines.

Table 3			
Radial	Velocities of	V1334 Cyg	

BJD-2400000.5	V_1	Instr.	BJD-2400000.5	V_1	Instr.
(day)	$({\rm km}~{\rm s}^{-1})$		(day)	$({\rm km}~{\rm s}^{-1})$	
56496.018	0.683 ± 0.013	SOPHIE	56493.168	-2.082 ± 0.017	HERMES
56497.065	-7.105 ± 0.014	SOPHIE	56493.229	-2.651 ± 0.017	HERMES
56498.038	-5.153 ± 0.013	SOPHIE	56493.917	-7.496 ± 0.017	HERMES
56500.021	-4.386 ± 0.014	SOPHIE	56494.000	-7.555 ± 0.017	HERMES
56586.910	-9.291 ± 0.024	SOPHIE	56494.201	-7.175 ± 0.017	HERMES
56587.880	-8.900 ± 0.013	SOPHIE	56494.235	-7.101 ± 0.017	HERMES
56588.955	-2.648 ± 0.012	SOPHIE	56494.908	-3.740 ± 0.016	HERMES
56829.089	-10.946 ± 0.011	SOPHIE	56495.235	-1.540 ± 0.016	HERMES
56830.100	-17.562 ± 0.011	SOPHIE	56495.958	0.736 ± 0.017	HERMES
56831.091	-17.999 ± 0.021	SOPHIE	56496.055	0.588 ± 0.017	HERMES
57200.059	-15.583 ± 0.018	SOPHIE	56496.237	-0.136 ± 0.017	HERMES
57201.084	-14.880 ± 0.012	SOPHIE	56855.146	-14.091 ± 0.008	HERMES
57644.919	10.503 ± 0.011	SOPHIE	56856.156	-13.070 ± 0.008	HERMES
57649.968	5.864 ± 0.018	SOPHIE	56857.153	-20.297 ± 0.008	HERMES
55522.925	7.657 ± 0.017	HERMES	56858.150	-16.430 ± 0.008	HERMES
56096.209	10.746 ± 0.017	HERMES	56859.150	-11.935 ± 0.008	HERMES
56097.196	2.917 ± 0.017	HERMES	56860.154	-18.842 ± 0.008	HERMES
56098.189	5.372 ± 0.016	HERMES	56861.155	-18.484 ± 0.008	HERMES
56099.203	10.961 ± 0.016	HERMES	56862.149	-12.708 ± 0.007	HERMES
56488.993	0.782 ± 0.016	HERMES	56864.136	-20.193 ± 0.007	HERMES
56489.095	1.116 ± 0.016	HERMES	56864.219	-19.919 ± 0.007	HERMES
56489.193	1.258 ± 0.016	HERMES	56865.146	-14.547 ± 0.006	HERMES
56489.978	-3.563 ± 0.017	HERMES	56865.223	-14.083 ± 0.007	HERMES
56490.062	-4.360 ± 0.017	HERMES	56866.142	-13.293 ± 0.007	HERMES
56490.226	-5.724 ± 0.017	HERMES	56866.220	-13.844 ± 0.008	HERMES
56490.951	-7.091 ± 0.017	HERMES	57178.090	-14.217 ± 0.012	HERMES
56491.001	-6.878 ± 0.016	HERMES	57179.098	-9.793 ± 0.011	HERMES
56491.039	-6.721 ± 0.016	HERMES	57180.091	-16.895 ± 0.009	HERMES
56491.198	-5.855 ± 0.016	HERMES	57181.155	-15.587 ± 0.007	HERMES
56491.934	-1.301 ± 0.016	HERMES	57182.187	-9.629 ± 0.007	HERMES
56492.004	-0.835 ± 0.016	HERMES	58026.968	2.570 ± 0.026	HERMES
56492.041	-0.592 ± 0.016	HERMES	58035.037	9.640 ± 0.014	HERMES
56492.952	-0.433 ± 0.017	HERMES	58070.845	3.797 ± 0.022	HERMES
56493.000	-0.770 ± 0.017	HERMES	58071.917	9.969 ± 0.015	HERMES
56493.037	-1.013 ± 0.017	HERMES	58073.878	2.356 ± 0.017	HERMES

RVs were estimated using the cross-correlation method. We created our own weighted binary mask by selecting unblended lines from high-resolution synthetic spectra ($R \sim 120,000$) covering the wavelength range of 4500–6800 Å. The cross-correlation function is then fitted by a Gaussian whose minimum value gives an estimate of the RV. Uncertainties include photon noise and internal drift. In addition, the standard deviation of the residual of the pulsation fit was also quadratically added. Measurements are listed in Table 3. The ZP difference between the instruments has been estimated using the systemic velocity as follows. We first performed an orbital fit using only the SOPHIE data, then with only the HERMES ones. We measured a difference of 30 m s⁻¹, which we added to the SOPHIE measurements, taking Hermes data as the reference.

2.3. Ultraviolet Spectroscopy

Measuring the orbital velocity of the companion is also necessary to resolve the degeneracy between the distance and masses. Due to its early spectral type, the companion is best detected at UV wavelengths, which is only possible with the *HST* because of UV absorption by the Earth's atmosphere. Four observations were obtained with the Space Telescope Imaging Spectrograph (STIS) on board *HST*. We used the high-resolution echelle mode E140H in the wavelength region 1163–1357 Å. They were taken over three annual *HST* cycles. Two were made very close in time to determine whether the companion is itself a short-period binary. The exposure time for each was 1800 s. Data reductions were made in the same way as in Evans et al. (2018a). Briefly, for each epoch, the 49 echelle orders were combined into a single 1D spectrum using an appropriate blaze function. Then, interstellar lines, which are recognizably narrow compared with the stellar lines, were removed by interpolation.

The absolute stability of the STIS E140H wavelength scale over time can be checked by comparing the wavelengths of interstellar features in different observations of the same star. Using these observations of V1334 Cyg and similar observations of the hot companion to S Mus, Proffitt et al. (2017) found the dispersion in the ZP of E140H velocity measurements to be about 0.24 km s^{-1} .

RVs of the companion were determined by cross-correlation. No synthetic template spectrum was used, instead we estimated a velocity difference with respect to the first observation by cross-correlating each of the spectra against it. This was typically done in 11 segments of approximately 10 Å, which were inspected to optimize the features so that a feature was not divided by a boundary. Mild smoothing was included (50 point smoothing) since the stellar features are broad. These velocity

Table 4 Differential Radial Velocities of the Companion of V1334 Cyg

MJD	ΔV_2 (km s ⁻¹)
56916.757	0.00 ± 0.51
56918.548 57251.901	$0.47 \pm 0.43 \\ -8.70 \pm 0.39$
57645.272	-28.36 ± 0.71

differences are directly used in our orbital model fitting. The uncertainties were derived from the differences between segments. Measurements are listed in Table 4.

3. Model Fitting and Orbital Solutions

We performed a combined fit of the interferometric orbit and RVs of the Cepheid and its companion. The fit includes three models with shared parameters for our three data sets. The first models the Cepheid RVs only (SOPHIE and HERMES data), i.e., the orbit around the system barycenter and the pulsation. The second models the companion's relative RVs (STIS data), i.e., the orbit of the secondary around the system barycenter. The last model fits the relative astrometric orbit of the companion determined from interferometry (MIRC data).

Our RV model of the primary star, the Cepheid, is defined as

$$V_1(t) = V_{1,\text{orb}} + V_{\text{puls}},$$

with the orbital RV $V_{1,orb}$ and the pulsation velocity V_{puls} , which are expressed with

$$V_{1,\text{orb}} = K_1[\cos(\omega + \nu) + e\cos\omega] + v_{\gamma},$$

$$V_{\text{puls}} = \sum_{i=1}^n [A_i\cos(2\pi i\phi_{\text{puls}}) + B_i\sin(2\pi i\phi_{\text{puls}})],$$

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with K_1 as the semi-amplitude of the Cepheids orbit due to the companion, ω the argument of periastron of the companions orbit, ν the true anomaly of the companion, e the eccentricity of the orbit, v_{γ} the systemic velocity, the pulsation phase $\phi_{\text{puls}} = (t - T_0) / P_{\text{puls}}$ (modulo 1), and (A_i, B_i) the amplitude of the Fourier series. The true anomaly is defined implicitly with the following three Keplerian parameters P_{orb} , T_p , e, and Kepler's equation

$$\tan \frac{\nu(t)}{2} = \sqrt{\frac{1+e}{1-e}} \tan \frac{E(t)}{2}$$
$$E(t) - e \sin E(t) = \frac{2\pi(t-T_p)}{P_{\text{orb}}},$$

where E(t) is the eccentric anomaly, T_p the time of periastron passage, t the time of the RV observations, and $P_{\rm orb}$ the orbital period.

Following the linear parametrization developed in Wright & Howard (2009) for $V_{1,orb}$, and including now the pulsation, our model can be simplified to

$$V_{1}(t) = C_{1} \cos \nu + C_{2} \sin \nu + v_{0} + \sum_{i=1}^{2} [A_{i} \cos(2\pi i \phi_{\text{puls}}) + B_{i} \sin(2\pi i \phi_{\text{puls}}), \qquad (1)$$

where we restricted the Fourier series to n = 2 as the pulsation curve is sinusoidal-like for such a short-period Cepheid (see also Figure 4). The parameters C_1 , C_2 , and v_0 are related to the Keplerian parameters through the relations (Wright & Howard 2009)

$$C_{1} = K_{1} \cos \omega,$$

$$C_{2} = -K_{1} \sin \omega,$$

$$v_{0} = v_{\gamma} + K_{1} e \cos \omega,$$

which can be converted back with (ω chosen so that sin ω has the sign of the numerator)

$$K_{1} = \sqrt{C_{1}^{2} + C_{2}^{2}},$$

$$\tan w = \frac{-C_{2}}{C_{1}},$$

$$v_{\gamma} = v_{0} - K_{1}e\cos\omega.$$

The fitted parameters are therefore defined as (C_1, C_2, C_3) $v_0, A_1, B_1, A_2, B_2, P_{\text{orb}}, T_p, e, P_{\text{puls}}$). T_0 is kept fixed in the fitting process to avoid degeneracy with T_p . The value is chosen such that $V_{\text{puls}}(0) = 0$.

For the second model, as we cross-correlated each STIS spectra with respect to the first observation, our relative RVs of the companion can be parameterized with

$$\Delta V_{2,\text{orb}}(t) = V_{2,\text{orb}}(t) - V_{2,\text{orb}}(t_0), \qquad (2)$$

$$V_{2,\text{orb}}(t) = \frac{K_1}{q} [\cos(\omega + \nu) + e \cos \omega] + v_{\gamma}, \qquad (3)$$

with the mass ratio $q = M_2/M_1$, and t_0 the time of the first STIS measurement. This adds the new parameter, q, as the fitted parameter.

Finally, the astrometric positions of the companion as measured from interferometry are modeled with the following equations (Heintz 1978):

$$\Delta \alpha = BX + GY,\tag{4}$$

$$\Delta \delta = AX + FY,\tag{5}$$

where (X, Y) are the elliptical rectangular coordinates defined as

$$X(t) = \cos E(t) - e$$
$$Y(t) = \sqrt{1 - e^2} \sin E(t).$$

The Thiele-Innes constants are parameterized in term of the orbital elements with

$$A = a_{as}(\cos \Omega \cos \omega - \sin \Omega \sin \omega \cos i),$$

$$B = a_{as}(\sin \Omega \cos \omega + \cos \Omega \sin \omega \cos i),$$

$$F = a_{as}(-\cos \Omega \sin \omega - \sin \Omega \cos \omega \cos i),$$

$$G = a_{as}(-\sin \Omega \sin \omega + \cos \Omega \cos \omega \cos i),$$

with a_{as} the angular semimajor axis in arcsecond (as), Ω the position angle of the ascending node, and *i* the orbital inclination, which are determined through the inversion



Figure 2. Result of our combined fit. Left: fitted (solid lines) and extracted primary (blue dots) and secondary (red dots) orbital velocity. Middle: fitted (solid line) and extracted (blue dots) pulsation velocity. Right: relative astrometric orbit of V1334 Cyg Ab.

relations

t

$$\tan(\Omega + \omega) = \frac{B - F}{A + G},$$

$$\tan(\Omega - \omega) = \frac{B + F}{A - G},$$

$$k_1 = \frac{1}{2}(A^2 + B^2 + F^2 + G^2),$$

$$k_2 = AG - BF,$$

$$a_{as}^2 = \sqrt{k_1^2 - k_2^2} + k_1 1$$

$$\cos i = \frac{k_2}{a_{as}^2},$$

with the quadrant of $\Omega \pm \omega$ determined from the sign of the numerators. These Thiele-Innes constants are included to the parameter list, giving a total of 16 variables to fit.

The distance and masses are then given by

$$K_{2} = \frac{K_{1}}{q},$$

$$a_{au} = \frac{9.191966 \times 10^{-5}(K_{1} + K_{2})P_{orb}\sqrt{1 - e^{2}}}{\sin^{3}i}$$

$$d = \frac{a_{au}}{a_{as}},$$

$$M_{T} = M_{1} + M_{2} = \frac{a^{3}d^{3}}{P_{orb}^{2}},$$

$$M_{1} = \frac{M_{T}}{1 + q},$$

$$M_{2} = q M_{1}.$$

with K_2 as the semi-amplitude of the companion, a_{au} the linear semimajor axis in astronomical unit (au), d the distance to the system, and M_1 and M_2 the Cepheid and companion mass, respectively.

We then applied a classical Monte chain Markov Carlo (MCMC) technique to fit the 16 model parameters characterizing the standard orbital elements and the pulsation of the Cepheid. Our best-fit values were obtained from the median values of the MCMC distribution (100,000 samples with uniform priors), while uncertainties were derived from the maximum value between the 16% and 84% percentiles. Our best fit is shown in Figure 2. We determined a distance of $d = 720.35 \pm 7.84$ pc ($\pm 1.1\%$), which is the most accurate model-independent distance of a Cepheid. This corresponds to a parallax of $\pi = 1.388 \pm 0.015$ mas. The two component masses were also determined with a high accuracy, $M_1 =$ $4.288 \pm 0.133 M_{\odot}$ ($\pm 3.1\%$) and $M_2 = 4.040 \pm 0.048 M_{\odot}$ $(\pm 1.2\%)$, with the primary star being the Cepheid. The other derived orbital and pulsation parameters are listed in Table 5.

Note that our orbit solutions are in rather good agreement with the previous estimates of the spectroscopic elements determined by Evans (2000; also listed in Table 5). It is worth mentioning that we did not use additional RV measurements from the literature for several reasons: (1) they are usually not very precise, (2) we wanted to use a data set as uniform as possible (i.e., RVs estimated the same way), (3) the effect on the RVs of a possible third component is reduced, and (4) we also avoid possible bias from the changing pulsation period of the Cepheid by limiting the time range.

4. Discussion and Conclusions

This is the first time that a binary Cepheid is resolved both spatially and spectroscopically. This provides the most accurate model-independent distance of a Cepheid, and the most precise masses for a Galactic Cepheid. Here we do not discuss or compare the evolutionary status of this system using our mass measurements as this can be found in Evans et al. (2018b).

With such a high distance accuracy, it is possible to test the agreement of V1334 Cyg with the existing calibrations of the P-L relations. We selected a sample of published relations in the V and K filters, as they are the most frequently used photometric bands (Sandage et al. 2004; Benedict et al. 2007; Fouqué et al. 2007; Storm et al. 2011; Groenewegen 2013; Gaia Collaboration et al. 2017).

This Cepheid is classified as pulsating in its first overtone, with a slightly shorter period than that in the fundamental mode. We therefore converted the period from the fundamental to the first overtone mode following the method used in Pilecki et al. (2018) with a pulsation model, and described in Taormina et al. (2018), resulting in an equivalent fundamental period of $P_0 = 4.7897 \pm$ 0.0322 days. The comparison with the empirical relation from Alcock et al. (1995), $P_1/P_0 = 0.720 - 0.027 \log P_0$, is very good with a relative difference <1% (or within 1.3σ).

THE ASTROPHYSICAL JOURNAL, 867:121 (9pp), 2018 November 10

Final Estimated Parameters of the V1334 Cyg Syste	n

	Pulsation		
$P_{\rm puls}$ (days)	3.33242 ± 0.00002		
T_0 (JD)	2 445 000.550		
$A_1 ({\rm km \ s}^{-1})$	-0.20 ± 0.35		
$B_1 ({\rm km \ s^{-1}})$	4.22 ± 0.04		
$A_2 ({\rm km s^{-1}})$	-0.01 ± 0.08		
$B_2 (\text{km s}^{-1})$	-0.42 ± 0.01		
	Orbit		
	Evans+ (2000)	This Work	
Porb (days)	1937.5 ± 2.1	1932.8 ± 1.8	
$T_{\rm p}$ (JD)	2443607 ± 14	2453316.75 ± 4.1	
e	0.197 ± 0.009	0.233 ± 0.001	
ω (°)	226.3 ± 2.9	229.8 ± 0.3	
$K_1 ({\rm km}{\rm s}^{-1})$	14.1 ± 0.1	14.168 ± 0.014	
$K_2 ({\rm km}{\rm s}^{-1})$		15.036 ± 0.304	
$v_{\gamma} (\mathrm{km s}^{-1})$	-1.8 ± 0.1	-2.65 ± 0.01	
Ω (°)		213.17 ± 0.35	
<i>i</i> (°)		124.94 ± 0.09	
a (mas)		8.54 ± 0.04	
a (au)		6.16 ± 0.07	
<i>d</i> (pc)		720.35 ± 7.84	
q		0.942 ± 0.020	
$M_1 (M_{\odot})$		4.288 ± 0.133	
$M_2 (M_{\odot})$		4.040 ± 0.048	

Note. Index 1 designates the cepheid and index 2 its main-sequence companion. Note that T_0 is kept fixed.

For each tested P-L relation, we determined the predicted absolute magnitudes for P_0 , which are represented in Figure 3 as black dots. We adopted as uncertainties the scatter of each relation given by the authors, which better represent the observed intrinsic dispersion (the width of the instability strip is the dominating uncertainty in the P-L relations; see e.g., Anderson et al. 2016a for a recent study). We derived the absolute magnitude with the usual relation $M_{\lambda} = m_{\lambda} - A_{\lambda}$ – $5 \log d + 5$, with m_{λ} the apparent magnitude at wavelength λ , A_{λ} the interstellar absorption parameter, and d the distance to the star. We corrected for the interstellar extinction, using $A_{\rm V} = 3.23E(B - V)$ and $A_{\rm K} = 0.119A_{\rm V}$ (Fouqué et al. 2007), with $E(B - V) = 0.025 \pm 0.009$ (Kovtyukh et al. 2008). For the V band, we estimated the weighted-mean apparent magnitude using a periodic cubic spline fit of four different published light curves (Szabados 1977; Henden 1980; Kiss 1998; Berdnikov 2008). The curve is shown in Figure 4. We determined the weighted-mean dereddenned magnitude of $m_{0,V} = 5.781 \pm 0.026$ mag, where the total uncertainty is estimated from the standard deviation of the residual values. There are no light curves available in the near-IR, so to estimate $m_{0,K}$ we used the value measured by 2MASS (Cutri et al. 2003). These observations were obtained at the pulsation phase of 0.36, very close to the phase of the mean radius (0.37), so that the magnitude variation is negligible (within the uncertainty). We estimated $m_{0,\mathrm{K}} = 4.451 \pm 0.036$ mag for the mean apparent magnitude in the K band. We then combined with our measured distance to estimate the absolute magnitudes M_{λ} , for which the total error bar includes the uncertainties on d, A_{λ} , and m_{λ} . Figure 3 shows the difference between M_{λ} of V1334 Cyg (red area) and the predicted values from literature P-L relations (black dots). However, the contribution of the companion must be subtracted from the combined magnitudes. To

correct from the flux contamination of the companion, we used the magnitude difference between the components estimated in V by Evans (1995), $\Delta V = 2.18$ mag, and from our measured H-band average flux ratio from interferometry for the K band, i.e., we assumed $\Delta K = \Delta H = 3.70 \pm 0.11$ mag. With our distance we can estimate the mean-corrected absolute magnitudes of the Cepheid to be $M_V(\text{cep}) = -3.37 \pm 0.05 \text{ mag}, M_H(\text{cep}) =$ -4.60 ± 0.05 mag, and $M_K(\text{cep}) = -4.80 \pm 0.04$ mag. Note that this is a rough estimate in K as we assumed the flux ratio to be the same as in H. From the magnitude differences, absolute magnitudes for the companion can also be derived, we found $M_V(\text{comp}) = -1.19 \pm 0.11 \text{ mag}, M_H(\text{comp}) = -0.90 \pm$ 0.12 mag, and $M_K(\text{comp}) = -1.10 \pm 0.12$ mag. The comparison of the $(V - H)_0$ color with the intrinsic color table of Pecaut & Mamajek $(2013)^{18}$ corresponds to a ~B7V companion of $\sim 3.9 M_{\odot}$ (the $(V - K)_0$ color is more uncertain as we assumed the same flux ratio in K and H). This is in good agreement with the spectral type estimate of Evans (1995; mean spectrum of a B7V star) and consistent with our measured mass.

The blue area in Figure 3 shows the absolute magnitudes of the Cepheid corrected from the flux contamination. We see in the optical band that the relations based on trigonometric parallax measurements (Benedict et al. 2007; Gaia Collaboration et al. 2017) are in agreement with the measured corrected absolute magnitude of the Cepheid. In the IR, the agreement is better, but still points to an offset, and again direct distance estimates seem to be more consistent. This can be explained by the fact that photometric measurements are more sensitive to a companion's flux contamination than they are to parallax observations, and therefore more strongly biased. The relation from Storm et al. (2011) is in marginal agreement, but also has a large uncertainty. In general, we see a systematic offset in P-L relations derived through photometric measurements (Baade-Wesselink method). In V, the average offset for photometric-based absolute magnitudes is only $\sim 1.5\sigma$, and $\sim 1.2\sigma$ for the K band. It is worth mentioning that increasing the value of E(B - V) would have the effect of increasing the inconsistency of our estimated absolute magnitude and the ones from the P-L relations plotted in Figure 3. We will also note that as V1334 Cyg is a first overtone pulsator, the amplitude in temperature can be neglected (\sim 240 K; Luck et al. 2008).

V1334 Cyg is a clear demonstration that Cepheid companions in binary systems are a significant source of a systematically positive photometric bias to the Cepheid fluxes, as well as contributors to the scattering of the P–L relations. In Figure 5 we show that correcting for the companion's flux brings the star closer to the position predicted by the P–L relations, with a stronger effect in V for this specific system. The same effect has been observed in the V and I band by Pilecki et al. (2018) in six LMC Cepheids in eclipsing binary systems.

Finally, the comparison of our orbital parallax with the second *Gaia* data release ($\pi = 1.151 \pm 0.066$ mas; Gaia Collaboration et al. 2018) shows a 3.6 σ deviation with our value. Correcting for the *Gaia* systematic offset of \sim -0.029 mas (estimated for quasars; Lindegren et al. 2018) still leaves a disagreement at 3.2 σ . This is however not surprising as binarity is not yet taken into account in the *Gaia* data reduction process. V1334 Cyg stands out as a demonstration that binarity can significantly impact Cepheid parallaxes. The selection criteria of Gaia Collaboration et al. (2017) of rejecting the known binary Cepheids seems like a

¹⁸ See also http://www.pas.rochester.edu/~emamajek/EEM_dwarf_UBVIJHK_ colors_Teff.txt.



Figure 3. Comparison between the absolute magnitudes of V1334 Cyg predicted from literature P–L relations (black dots) and the present distance measurement (red and blue areas) in two photometric bands. The blue and red areas represent the measured absolute magnitude with and without the subtraction of the companion's flux contamination, respectively. In the K band, these two regions overlap as the contribution of the companion is smaller.



Figure 4. Interpolated V-band light curve of V1334 Cyg.

good approach, as seen in our Figure 3 with a good agreement in V band between the expected value and our measured corrected absolute magnitude. The final *Gaia* data release with hundreds of Galactic Cepheid parallaxes promises to constrain the ZP of P–L relations to an exquisite precision. But reddening corrections, biases from orbiting companions (astrometric and photometric), as well as the flux contribution of circumstellar envelopes will



Figure 5. Period–Luminosity relations constructed from direct parallax measurements. This includes our measured distance and those from Casertano et al. (2016), Riess et al. (2018), and Benedict et al. (2007, 2002). We also included the distance estimated from light echoes by Kervella et al. (2014). The blue and red dots represent the location of V1334 Cyg for companion-flux corrected and uncorrected magnitude, respectively. Uncertainty on the fundamentalized period is also shown. The relation derived by Benedict et al. (2007) is also plotted, with the rms of the residuals in the shaded area.

limit the accuracy of the P–L relation calibration if not properly taken into account.

This research is based on observations made with SOPHIE spectrograph on the 1.93-m telescope at Observatoire de Haute Provence (CNRS/AMU), France (ProgID: 13A.PNPS10, 13B.

PNPS003, 14A.PNPS010, 15A.PNPS010, 16B.PNPS.KERV). This research is based on observations made with the Mercator Telescope, operated on the island of La Palma by the Flemish Community, at the Spanish Observatorio del Roque de los Muchachos of the Instituto de Astrofsica de Canarias. HERMES is supported by the Fund for Scientific Research of Flanders (FWO), Belgium; the Research Council of K.U. Leuven, Belgium; the Fonds National de la Recherche Scientifique (F.R.S.- FNRS), Belgium; the Royal Observatory of Belgium; the Observatoire de Genve, Switzerland; and the Thüringer Landessternwarte, Tautenburg, Germany. This work is also based on observations with the NASA/ESA Hubble Space Telescope obtained at the Space Telescope Science Institute, which is operated by the Association of Universities for Research in Astronomy, Inc., under NASA contract NAS5-26555 (ProgID 13454). We acknowledge the support of the French Agence Nationale de la Recherche (ANR-15-CE31-0012-01, project Unlock-Cepheids). W.G. and G.P. gratefully acknowledge financial support from the BASAL Centro de Astrofisica y Tecnologias Afines (CATA, AFB-170002). W.G. also acknowledges financial support from the Millenium Institute of Astrophysics (MAS) of the Iniciativa Cientifica Milenio del Ministerio de Economia, Fomento y Turismo de Chile (project IC120009). We acknowledge financial support from the Programme National de Physique Stellaire (PNPS) of CNRS/INSU, France. Support from the Polish National Science Centre grants MAESTRO UMO-2017/26/A/ST9/00446 and from the IdP II 2015 0002 64 grant of the Polish Ministry of Science and Higher Education is also acknowledged. The research leading to these results has received funding from the European Research Council (ERC) under the European Union's Horizon 2020 research and innovation programme (grant agreement No. 695099 and 639889). N.R.E. acknowledges support from the Chandra X-ray Center NASA (contract NAS8-03060) and the HST grants GO-13454.001-A and GO-14194.002. This work is based upon observations obtained with the Georgia State University Center for High Angular Resolution Astronomy Array at Mount Wilson Observatory. The CHARA Array is supported by the National Science Foundation under grant No. AST-1211929, 1411654, and 1636624. Institutional support has been provided from the GSU College of Arts and Sciences and the GSU Office of the Vice President for Research and Economic Development. B.P. acknowledges financial support from the Polish National Science Center grant SONATA 2014/15/D/ST9/02248.

Facilities: HST(STIS), CHARA(MIRC), OHP:1.93m (SOPHIE), Mercator:1.2m (HERMES).

Software: Candid (Gallenne et al. 2015), Emcee (Foreman-Mackey et al. 2013), SearchCal (Bonneau et al. 2006), MIRC pipeline (Monnier et al. 2007).

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